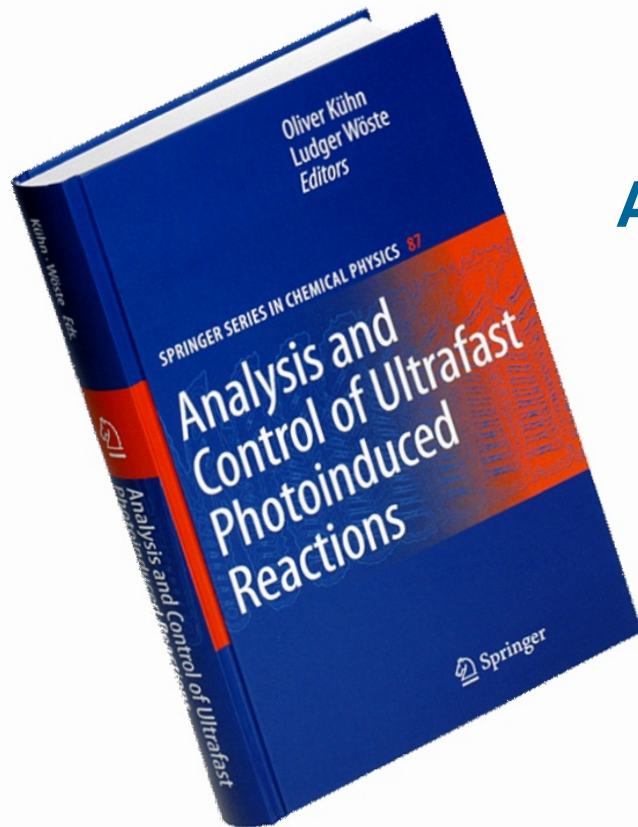
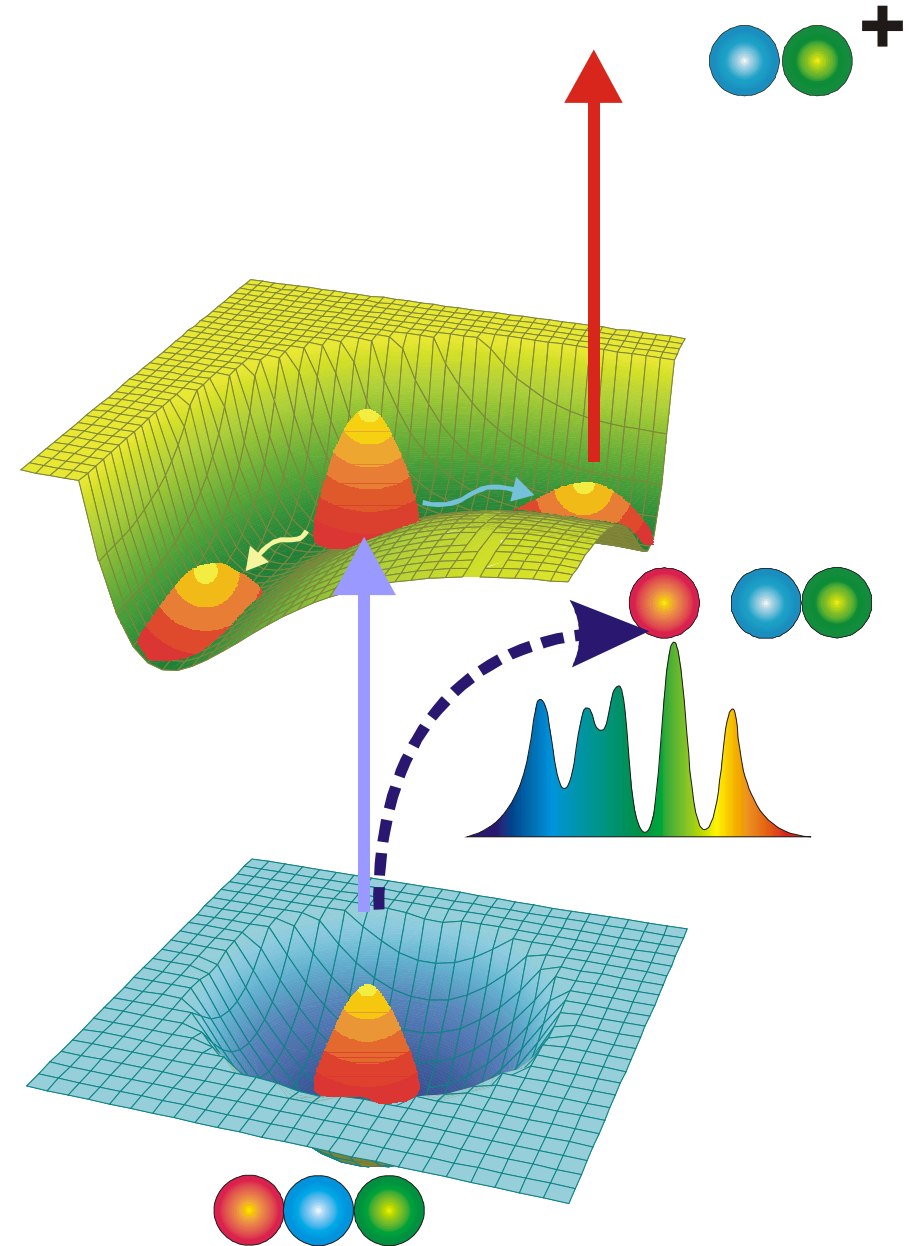


# Laser Pulse Control of Ultrafast Transfer Processes in Molecular Nanostructures

Volkhard May, Institute of Physics  
Humboldt-University at Berlin

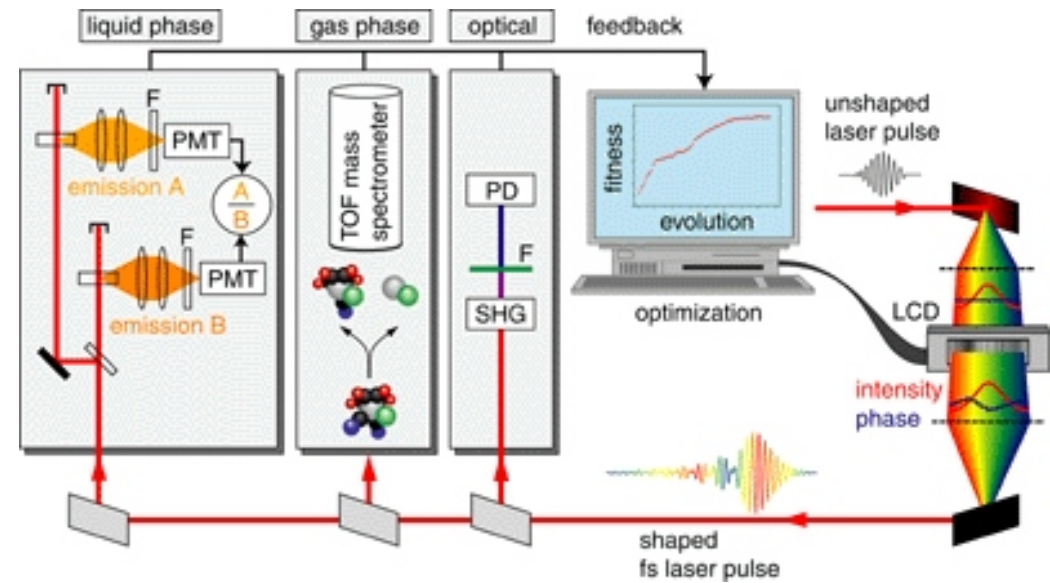


**Acknowledgment:**  
T. Mancal  
B. Brüggemann  
A. Kaiser  
L. Wang  
DFG (Sfb 450)



# Experiment

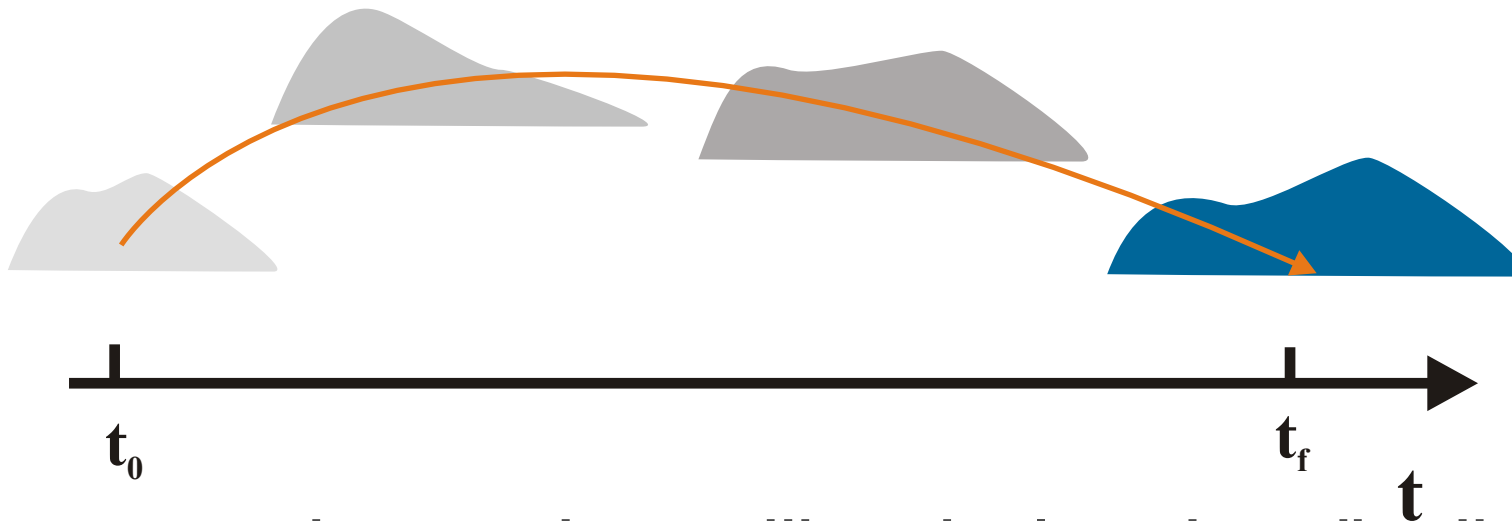
## Adaptive Femtosecond Quantum Control



G. Gerber

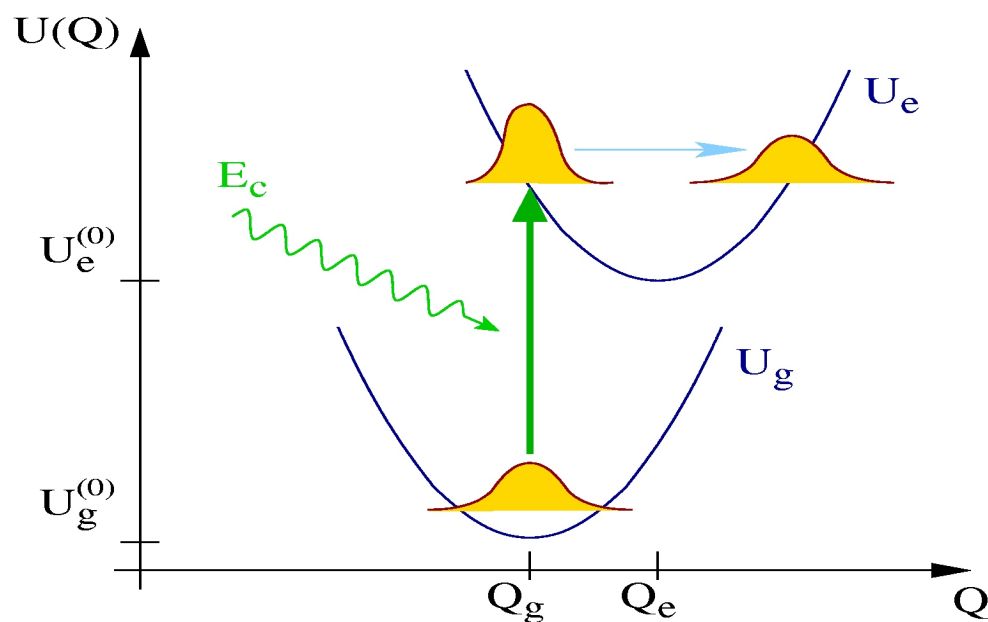
# Theory

## Optimal Control Theory



- gas-phase systems with a single or two vibrational DOF
- account for laser field fluctuations and intensity profile
- a single DOF coupled to a heat bath
- random orientation
- static disorder
- optimization of an observable
- control of particle motion

# A Simple Example



Two level model with harmonic PES.

– **Initial state:**

$$|\psi_0\rangle = |\phi_g\rangle |\chi_{g,0}\rangle$$

– **Target state:**

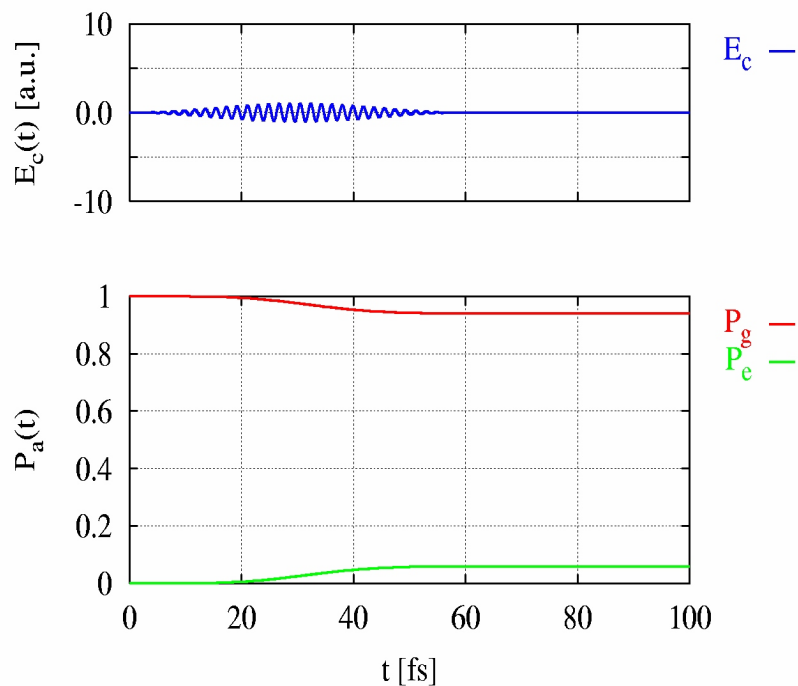
$$|\psi_{\text{tar}}\rangle = |\phi_e\rangle |\chi_{\text{tar}}\rangle$$

– **Target time:**

$$t_f = 100 \text{ fs}$$

–  $J_0[\mathbf{E}_c] = |\langle \psi_{\text{tar}} | \psi(t_f) \rangle|^2$

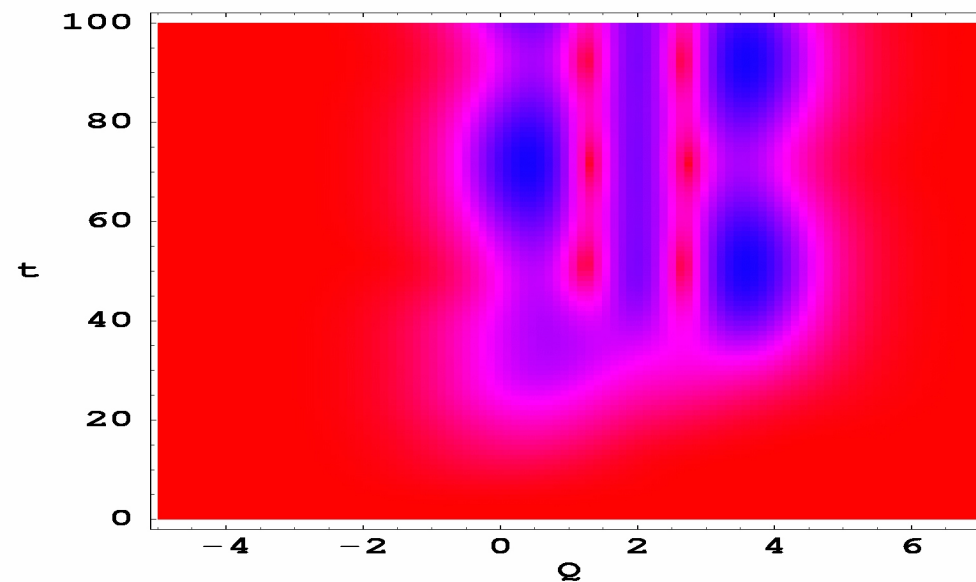
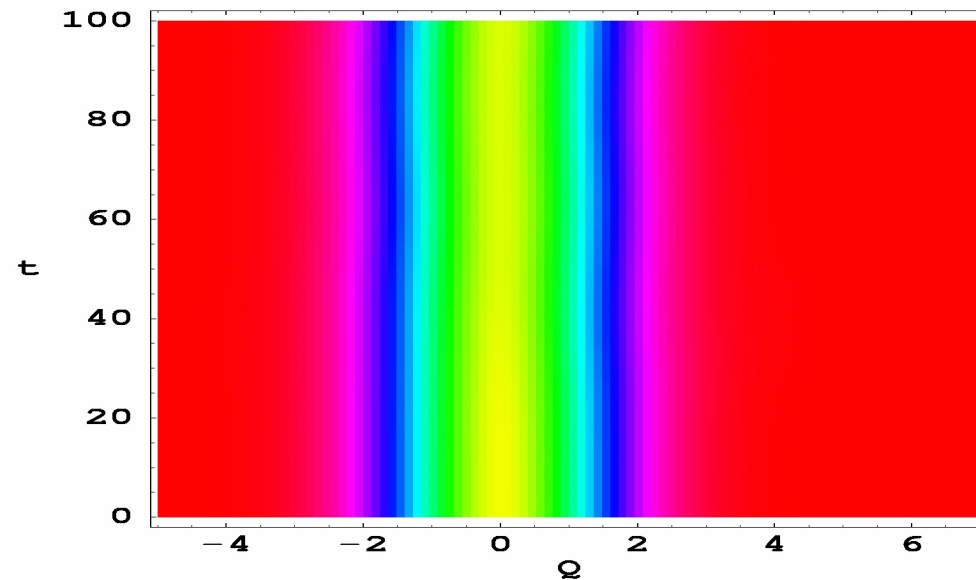
## Zeroth iteration:



Control field (upper panel) and state population (lower panel).

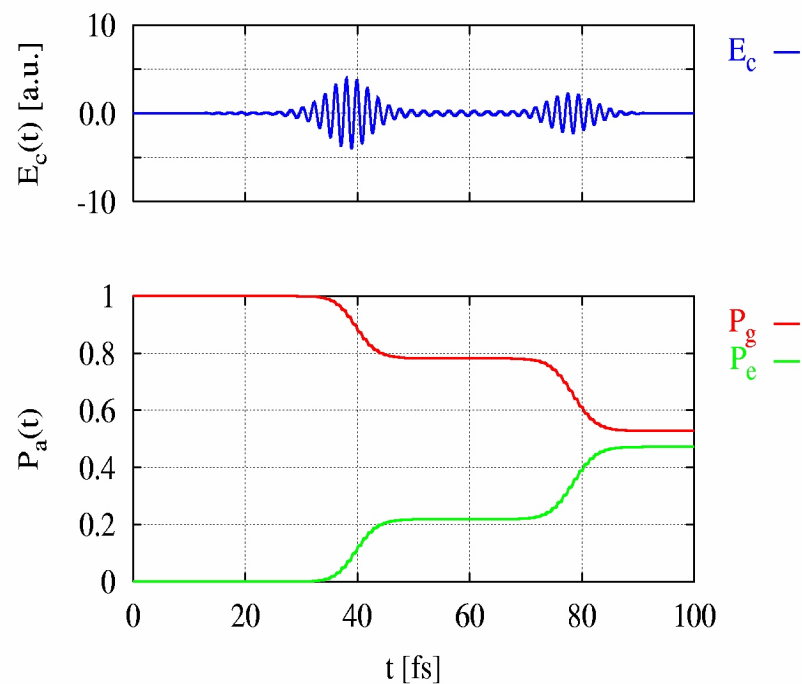
- Control yield

$$J_0^{(0)} = |\langle \psi_{\text{tar}} | \psi^{(0)}(t_f) \rangle|^2 = 0.02.$$



Vibrational wavepacket, ground state (upper panel), excited state (lower panel).

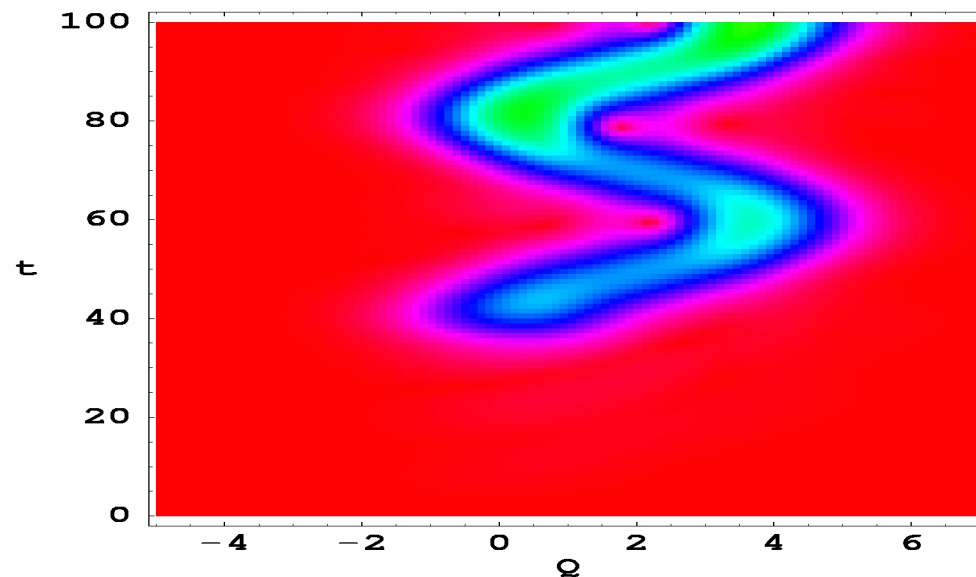
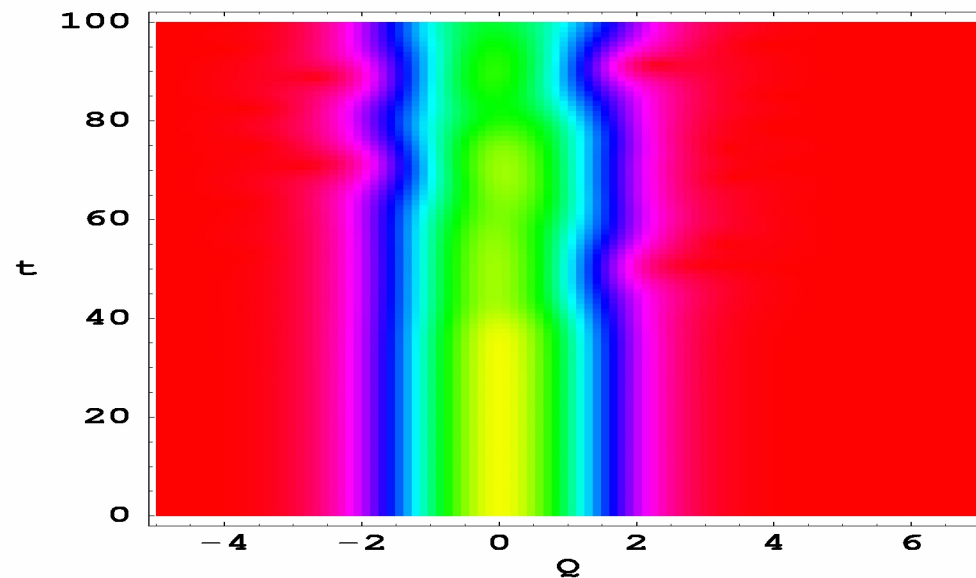
## First iteration:



Control field (upper panel) and state population (lower panel).

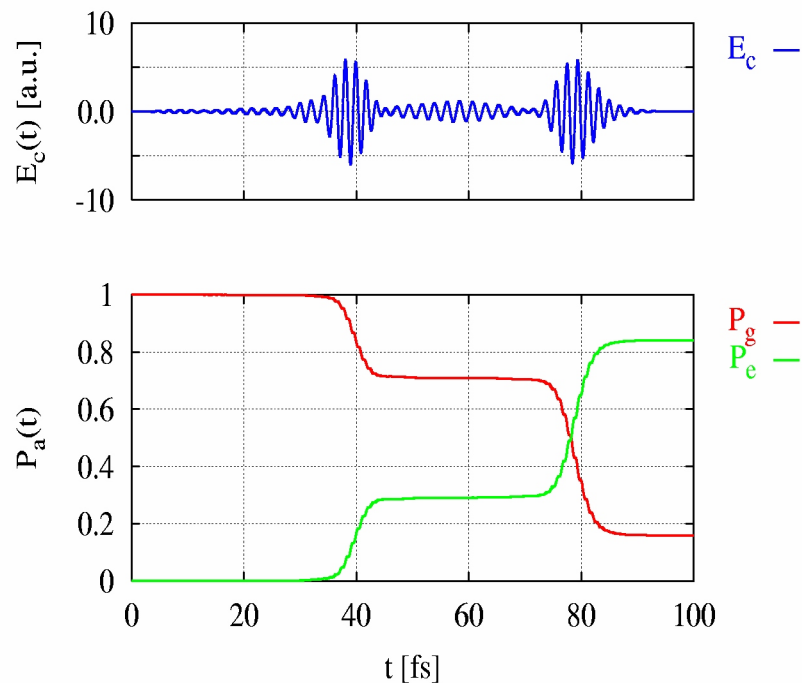
### ● Control yield

$$J_0^{(1)} = |\langle \psi_{\text{tar}} | \psi^{(1)}(t_f) \rangle|^2 = 0.43.$$



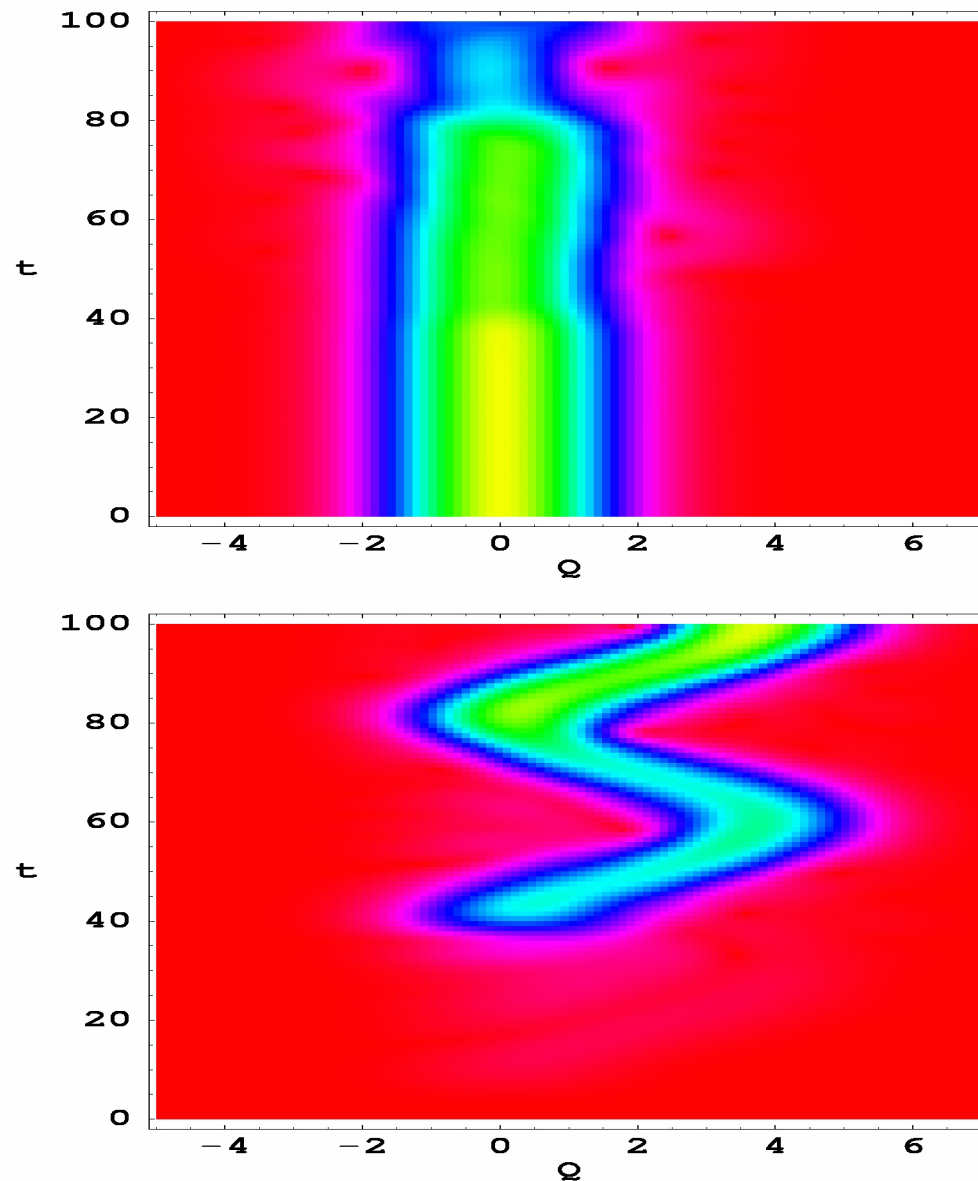
Vibrational wavepacket, ground state (upper panel), excited state (lower panel).

## Third iteration:

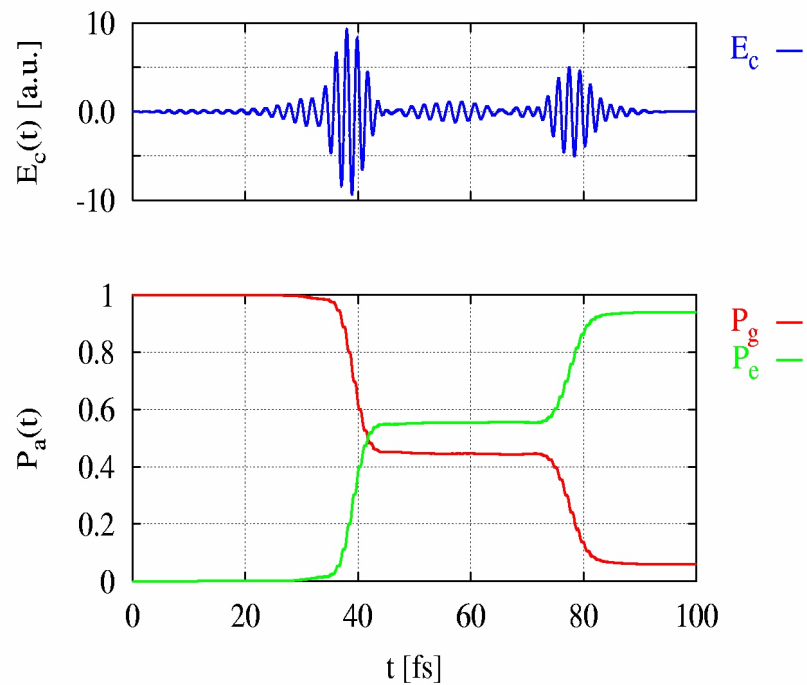


- Control yield

$$J_0^{(3)} = |\langle \psi_{\text{tar}} | \psi^{(3)}(t_f) \rangle|^2 = 0.81.$$



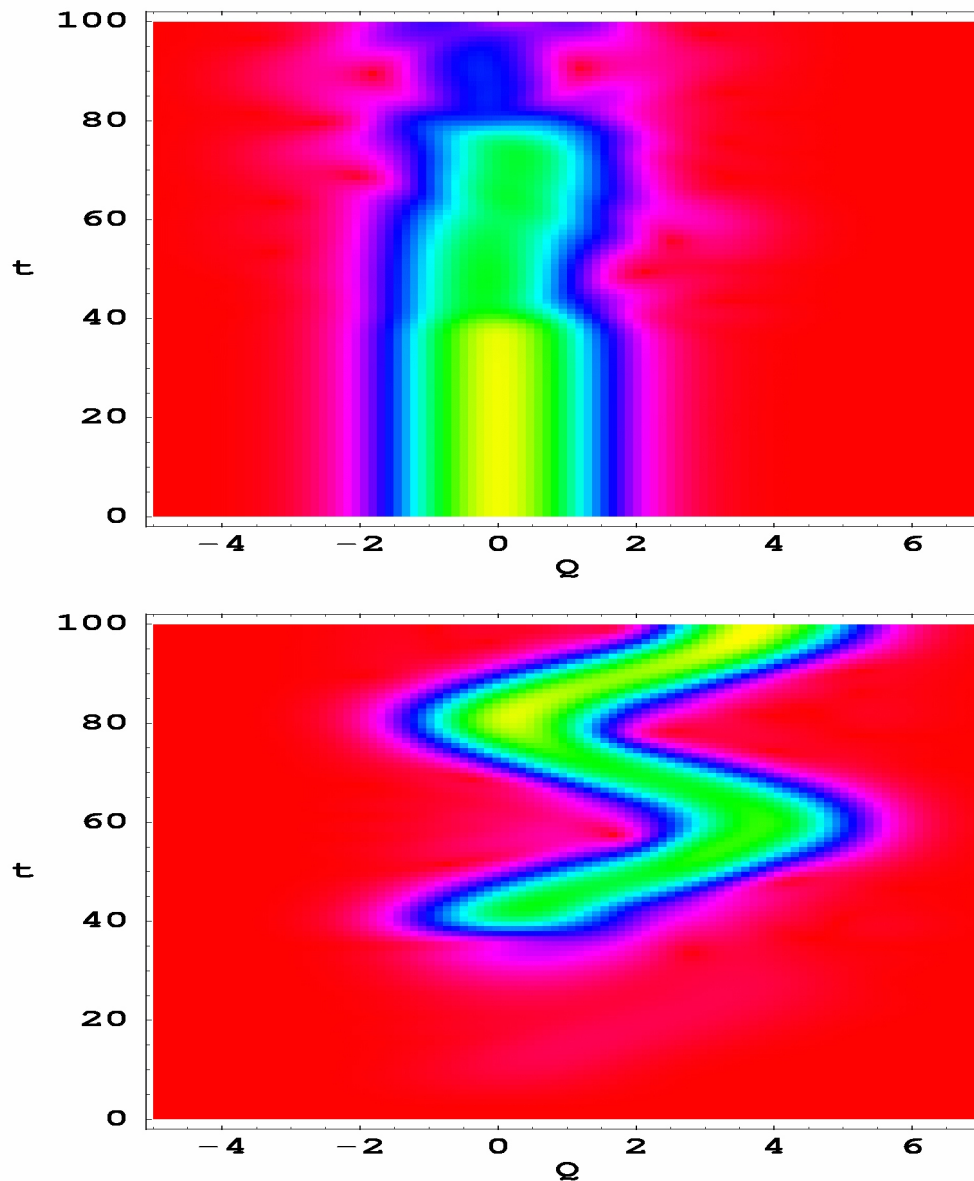
## 20th iteration:



Control field (upper panel) and state population (lower panel).

### ● Control yield

$$J_0^{(20)} = |\langle \psi_{\text{tar}} | \psi^{(20)}(t_f) \rangle|^2 = 0.92.$$



Vibrational wavepacket, ground state (upper panel), excited state (lower panel).



# Optimal Control Theory

Control functional

$$J[\mathbf{E}_c] = \mathcal{O}[\mathbf{E}_c] - \lambda \left( \frac{1}{2} \int_{t_0}^{t_f} dt \mathbf{E}_c^2(t) - I_0 \right)$$

Functional equation  
determining the optimal pulse

$$\mathbf{E}_c(t) = \lambda \frac{\delta \mathcal{O}[\mathbf{E}_c]}{\delta \mathbf{E}_c(t)}$$

## SOLUTION OF THE CONTROL PROBLEM

Control Functional

$$J[\mathbf{E}_c] = |\langle \Psi_{\text{tar}} | \Psi(t_f; \mathbf{E}_c) \rangle|^2 - \frac{\lambda}{2} \int_{t_0}^{t_f} dt \mathbf{E}_c^2(t)$$

Self-Consistency Equation for the Optimal Field

$$\mathbf{E}_c(t) = \frac{i}{\hbar\lambda} (\langle \Psi(t_f; \mathbf{E})_{\text{tar}} | \Psi_c \rangle \langle \Psi_{\text{tar}} | U(t_f, t; \mathbf{E}_c) \hat{\mu} U(t, t_0; \mathbf{E}_c) | \Psi(t_0) \rangle + \text{c.c.})$$

Coupled Forward-Backward Propagation

$$i\hbar \frac{\partial}{\partial t} |\Psi(t)\rangle = (H_{\text{mol}} - \mathbf{E}_c(t)\hat{\mu}) |\Psi(t)\rangle$$

$$i\hbar \frac{\partial}{\partial t} |\Theta(t)\rangle = (H_{\text{mol}} - \mathbf{E}_c(t)\hat{\mu}) |\Theta(t)\rangle$$

# **FIRST EXAMPLE**

# Complexity of the Control Task

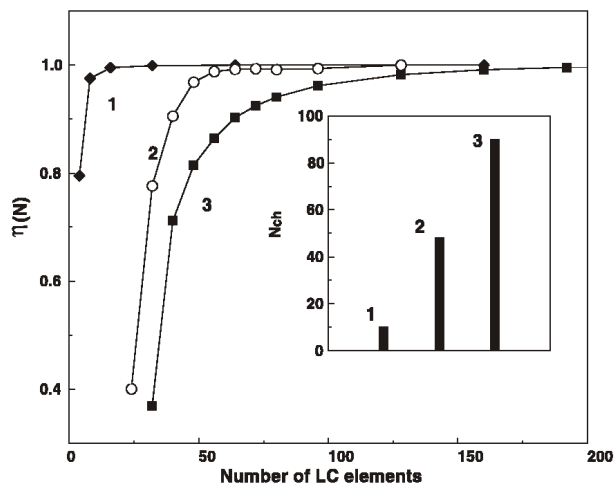
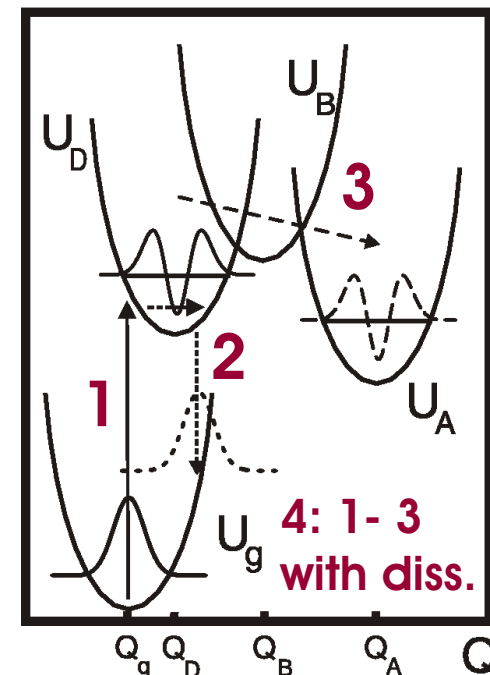
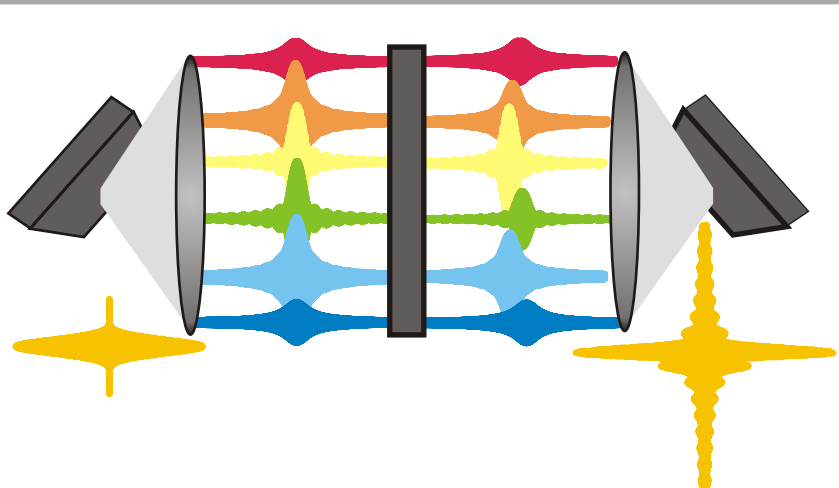


Fig. 3. The efficiency of the pulse shaper characterized by the ratio  $\eta$  versus the number  $N$  of liquid crystal cells in the shaper for the different control tasks of Fig. 1. Inset:  $N_{ch}$  leading to a 95% yield ordered with respect to the different control tasks.

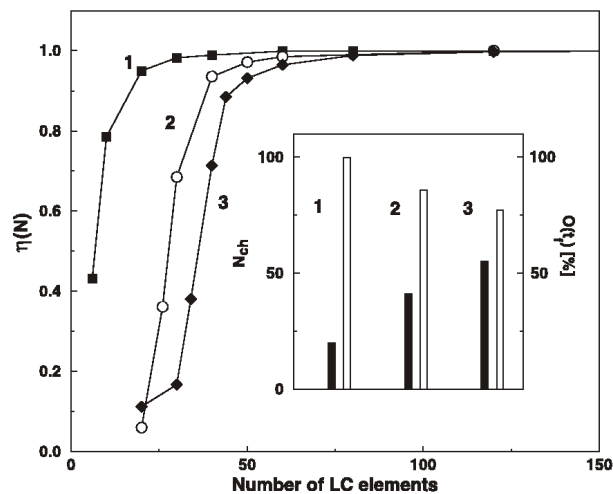


Fig. 4. The efficiency of the pulse shaper as shown in Fig. 3, but for the control task 4, and with different strength of dissipation. The vibrational life-time of the target level  $\tau_t$  is used to characterize the strength of dissipation. 1. Without dissipation, 2.  $\tau_t = 320$  fs, 3.  $\tau_t = 640$  fs. Inset:  $N_{ch}$  as in Fig. 3 (black bar) and the population of the target state in percentage (white bar).

T. Mancal and V. M.,  
CPL 362, 407 (2002)

# **SECOND EXAMPLE**

# Optimal Control Theory for Non-Resonant Multi-Photon Transitions

Standard scheme of OCT  
using a target operator

$$\mathcal{O}[\mathbf{E}_c] = \langle \Psi(t; \mathbf{E}_c) | \hat{O} | \Psi(t; \mathbf{E}_c) \rangle$$



# Non-Resonant Two-Photon Transitions

# The RWA and the SVA

Coupled Schrödinger-equations for the vibrational wave functions

$$\begin{aligned}i\hbar \frac{\partial}{\partial t} |\chi_g(0; t)\rangle &= (H_g - \frac{1}{2}|E(t)|^2 d_{gg}^{(II)}) |\chi_g(0; t)\rangle - \frac{1}{4} E^{*2}(t) d_{ge}^{(II)} |\chi_e(2; t)\rangle \\i\hbar \frac{\partial}{\partial t} |\chi_e(2; t)\rangle &= (H_e - 2\hbar\omega_0 - \frac{1}{2}|E(t)|^2 d_{ee}^{(II)}) |\chi_e(2; t)\rangle - \frac{1}{4} E^2(t) d_{eg}^{(II)} |\chi_g(0; t)\rangle\end{aligned}$$

## Control Functional

$$J(t_f; E, E^*) = | \langle \chi_e^{(\text{tar})} | \chi_e(t_f) \rangle |^2 - \frac{\lambda}{4} \int_{t_0}^{t_f} dt |E(t)|^4$$

**D. Ambrosek, M. Oppel, L. Gonzalez and V. M.,  
special issue, Opt. Comm. 264, 502 (2006).**

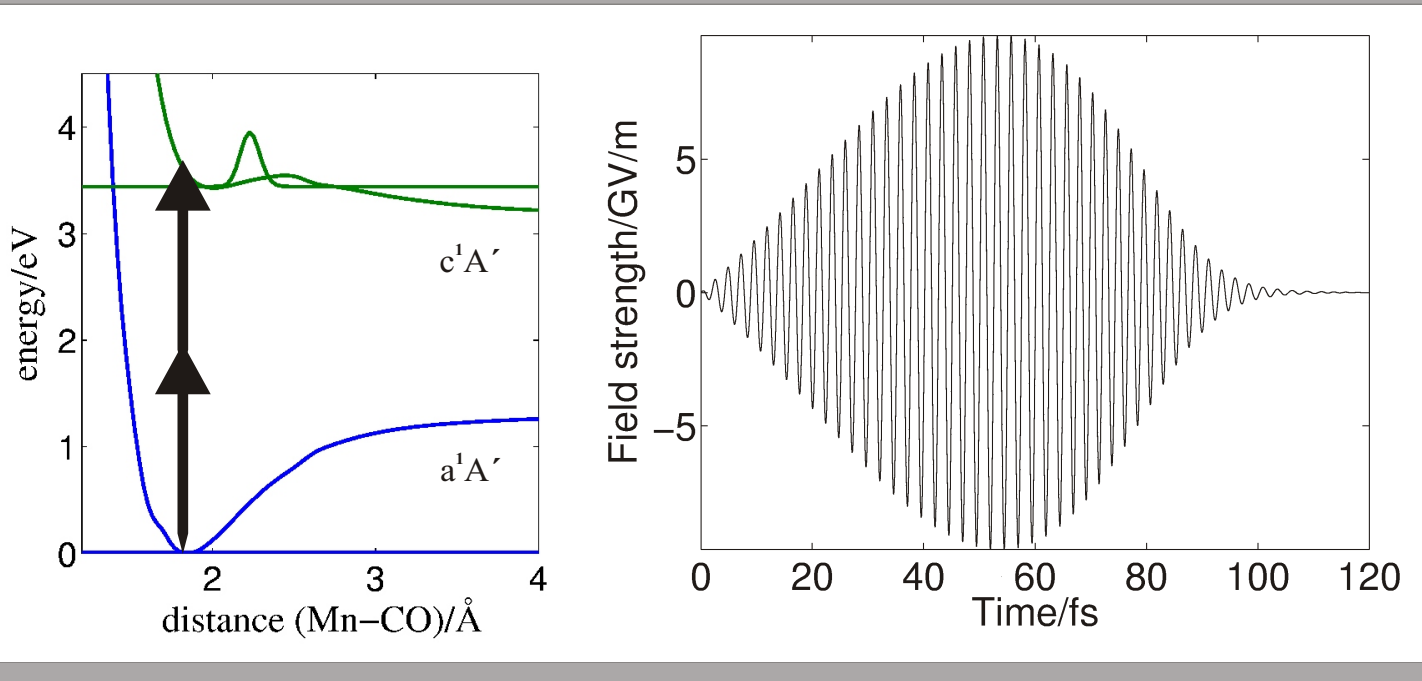


TABLE I: The yield  $Q$ , the renormalized yield  $q$ , the maximum  $E_{\max}$  of the field-strength (in GV/m) and the related intensity  $I_{\max}$  (in  $\text{GW}/\text{cm}^2$ ) for different used penalty factors  $\lambda$  (in  $10^{12}$  fs  $(\text{GV}/\text{m})^4$ ) of the described control scheme

$Q$	$q$	$E_{\max}$	$I_{\max}$	$\lambda$
0.68	0.82	58.1	3.02	3
0.29	0.74	42.2	2.19	12
0.0049	0.72	14.7	0.76	19
0.0009	0.72	9.6	0.50	20



# **THIRD EXAMPLE**

# OCT with a target operator distributed in time and parameter space

$$\mathcal{O}[\mathbf{E}_c] = \int_{t_0}^{\infty} dt \int dp \langle \Psi(t; p) | \hat{O}(t; p) | \Psi(t; p) \rangle$$

Shi, Rabitz, JCP 92, 364 (1990), 97, 276 (1992)

direct optimization of transient probe pulse absorption in  
a pump-probe scheme

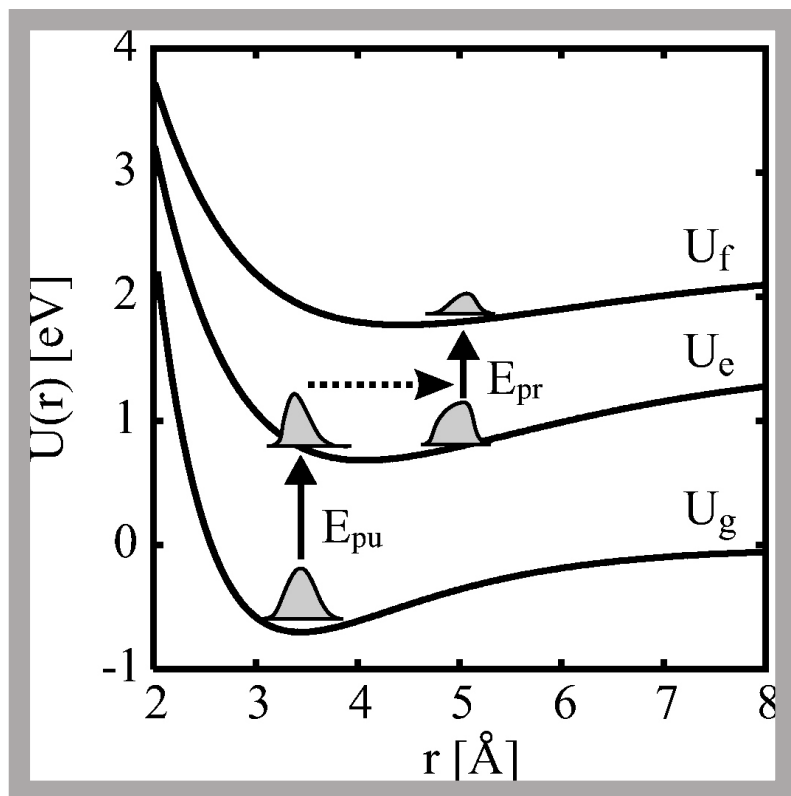
A. Kaiser, and V. M., JCP 121, 2528 (2004), CPL 405, 339 (2005),  
CP 320, 95 (2006)

consideration of structural and energetic disorder

**Direct Optimization  
of a Probe-Pulse  
Transient Absorption**

# Three level scheme for NaK

- 1<sup>1+</sup> - ground-state
- 2<sup>1+</sup> - first-excited states
- 3<sup>1+</sup> - higher excited state



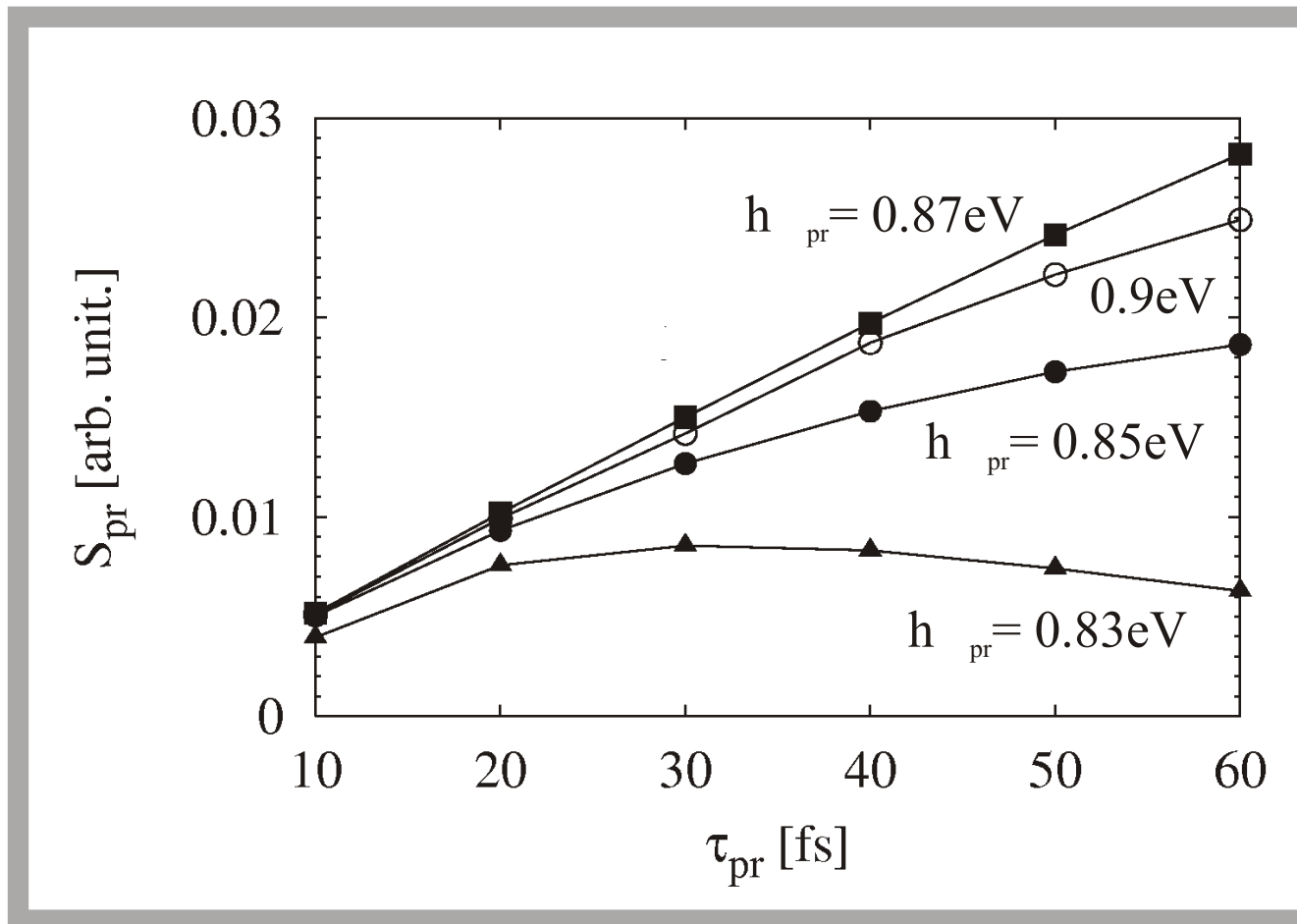
**probe pulse  
transient absorption signal**

$$S_{\text{pr}} = - \int dt \frac{\partial \mathbf{E}_{\text{pr}}(t)}{\partial t} \mathbf{P}_{\text{pr}}(t; \mathbf{E}_{\text{c}})$$

$$\mathbf{P}_{\text{pr}}(t) = n_{\text{mol}} \langle \Psi(t; \mathbf{E}_{\text{c}}, \mathbf{E}_{\text{pr}}) | \hat{\mu} | \Psi(t; \mathbf{E}_{\text{c}}, \mathbf{E}_{\text{pr}}) \rangle - n_{\text{mol}} \langle \Psi(t; \mathbf{E}_{\text{c}}) | \hat{\mu} | \Psi(t; \mathbf{E}_{\text{c}}) \rangle$$

**probe pulse  
polarization**

# Optimized Probe Pulse Transient Absorption Signal versus Probe Pulse Length



- > control pulse acts up to 1.5 ps
- > probe pulse is centered at 1.6 ps

A. Kaiser, and V. M., JCP 121, 2528 (2004), CPL 405, 339 (2005), CP (2005)

# **FOURTH EXAMPLE**

# OCT for open system dynamics

$$\mathcal{O}[\mathbf{E}_c] = \text{tr}\{\hat{\rho}(t_f; \mathbf{E}_c)\hat{O}\}$$

$$\mathbf{E}_c(t) = \frac{i}{\hbar\lambda} \text{tr}\{\hat{O}\mathcal{U}(t_f, t; \mathbf{E}_c) [\hat{\mu}, \hat{\rho}(t; \mathbf{E}_c)]_-\}$$

**Bartana, Kosloff, Tannor, JCP 106, 1435 (1997)**

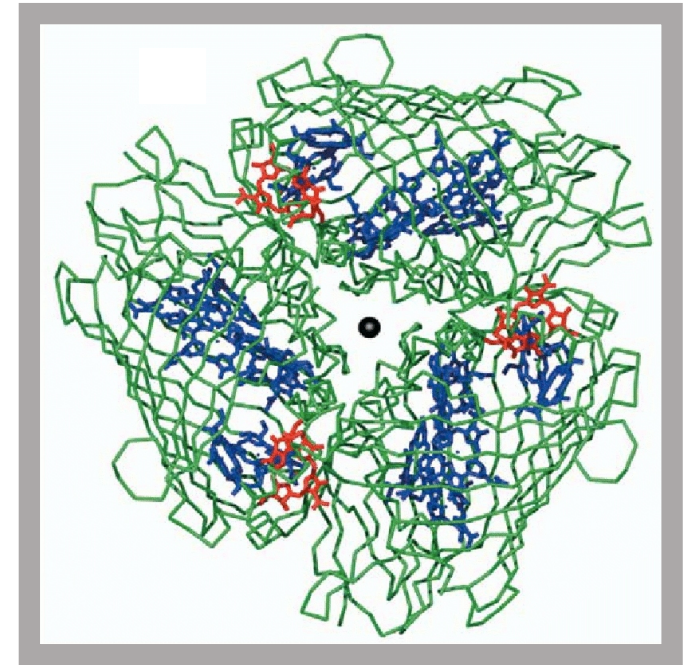
**Ohtsuki, Yhu, Rabitz, JCP 110, 9825 (1999)**

**Mancal, Kleinekathöfer, May, JCP 117, 636 (2002)**

**Xu, Yan, Ohtsuki, Fujimura, Rabitz, JCP 120, 6600 (2004)**

**Brüggemann, May, JPCB 108, 10529 (2004)**

# Excitation Energy Localization in a Pigment Protein Complex



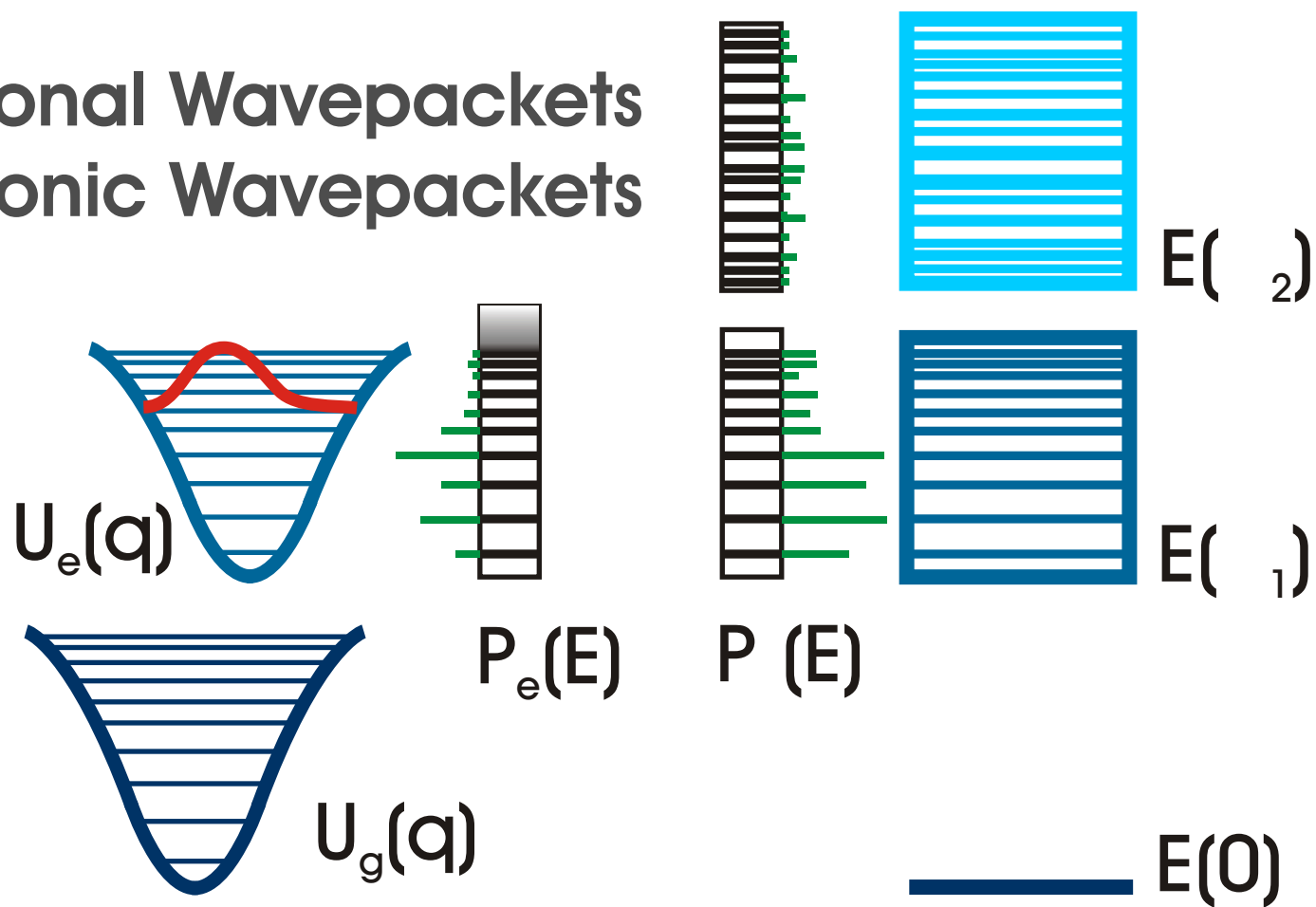
$$\mathcal{O}[\mathbf{E}_c] = \text{tr}\{\hat{\rho}(t; \mathbf{E}_c)\hat{O}\}$$

$$\mathcal{O}[\mathbf{E}_c] = \int_{t_0}^{\infty} dt \int dp \langle \Psi(t; p) | \hat{O}(t; p) | \Psi(t; p) \rangle$$



# Excitation Energy Localization via the Formation of Excitonic Wavepackets

Vibrational Wavepackets  
versus Excitonic Wavepackets



The study of particular relaxation pathways  
may become possible!

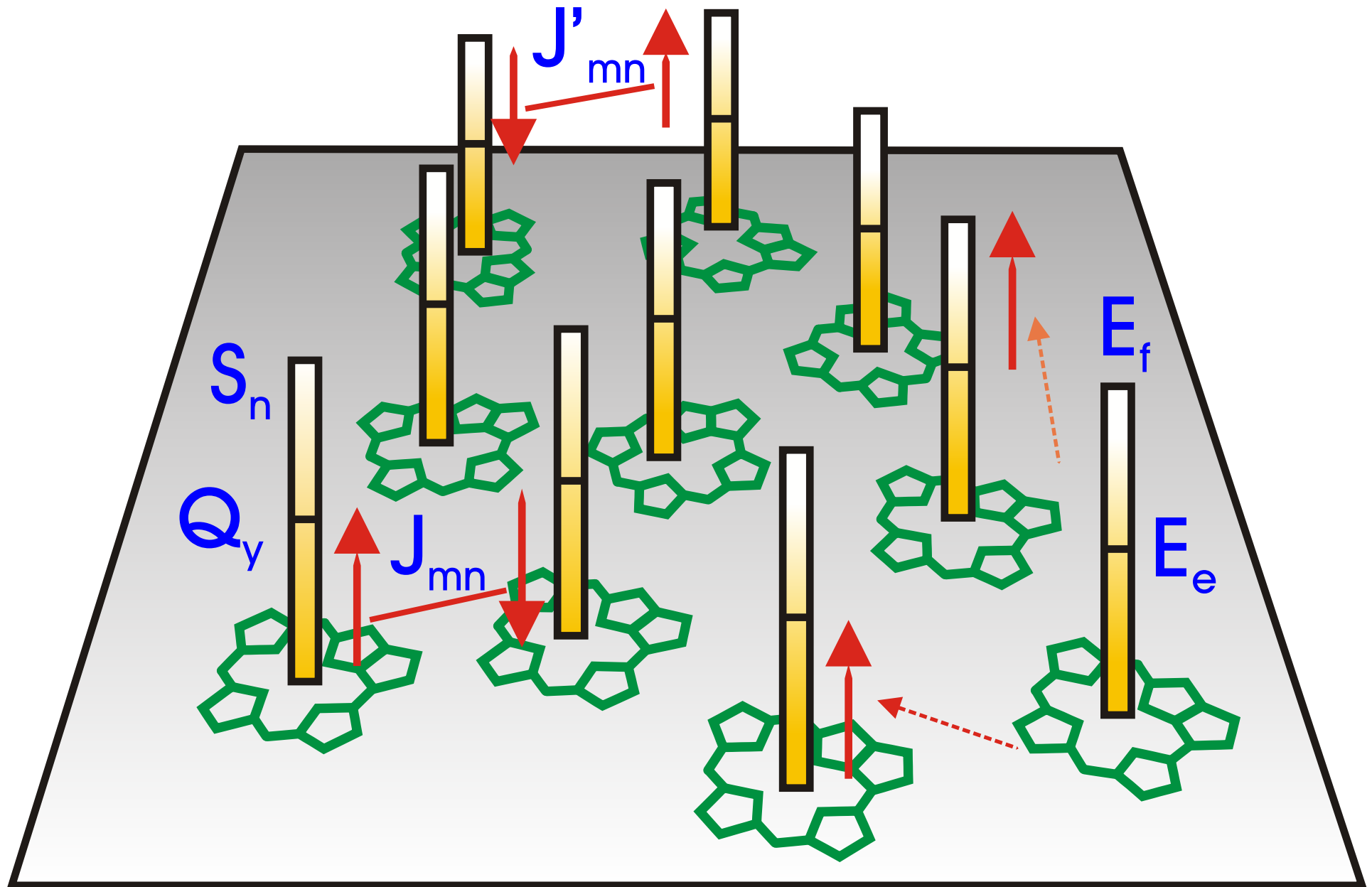
## Simulating femtosecond dynamics of excitons in chromophore complexes:

- formation of single- and two-exciton states
- electronic excitation energy dissipation
- presence of static disorder

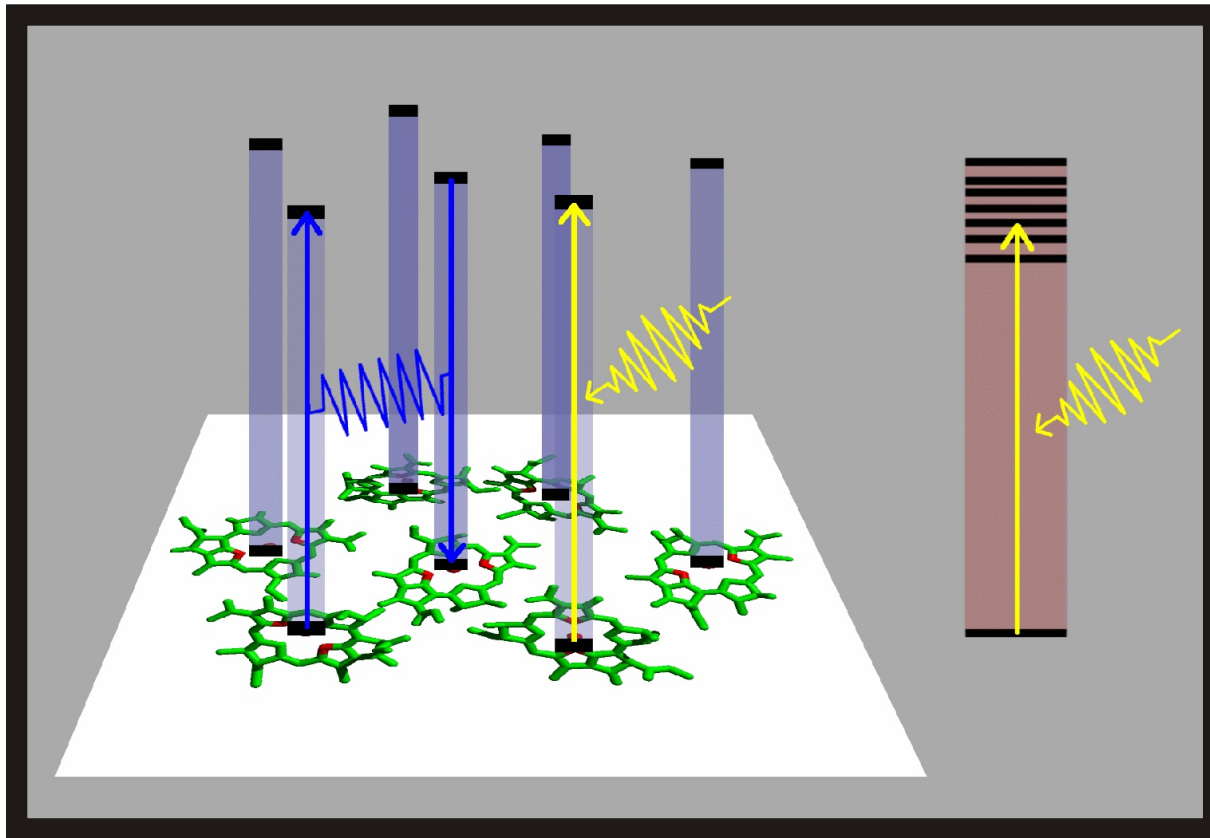
*ab initio* description of the single-exciton states possible (Schulten, 1998, ...)

description of all other effects requires the introduction of certain models

# Electronic Level Scheme



# Formation of Delocalized Single- and Two-Exciton States



ground-state

$$|\alpha_0\rangle = \prod_m |\varphi_{mg}\rangle$$

single exciton state

$$|\alpha_1\rangle = \sum_m C(\alpha_1; m) |\phi_m\rangle$$

two-exciton state

$$|\alpha_2\rangle = \sum_{m,n} C(\alpha_2; mn) |\phi_{mn}\rangle$$

Th. Renger, V. M., and O. Kühn,  
Phys. Rep. 343, 137 (2001)

# Excitonic Wavepacket

$$|\alpha\rangle = \sum_m C_\alpha(m) |\phi_m\rangle \quad \Longrightarrow \quad |\phi_{m_{\text{tar}}}\rangle = \sum_\alpha C_\alpha^*(m_{\text{tar}}) |\alpha\rangle$$

## Linear response expression for the driven wave function

$$|\phi_{m_{\text{tar}}}\rangle = |\Psi(t_f)\rangle \approx \frac{i}{\hbar} \sum_\alpha \int_{t_0}^{t_f} d\bar{t} e^{-i\Omega_\alpha(t-\bar{t})} \mathbf{d}_\alpha \mathbf{E}(\bar{t}) |\alpha\rangle \approx \frac{i}{\hbar} \sum_\alpha e^{-i\Omega_\alpha t} \mathbf{d}_\alpha \mathbf{E}(\Omega_\alpha) |\alpha\rangle$$

## Estimate of the Control Field

$$\mathbf{E}(t) \approx -i\hbar \sqrt{\mathcal{N}} f(t) \mathbf{e} \sum_\alpha e^{-i\Omega_\alpha(t-t_f)} \frac{C_\alpha^*(m_{\text{tar}})}{d_\alpha} + \text{c.c.}$$

## Optimization of the target chromophor population

$$P_{m_{\text{tar}}}(t_f) = \frac{1}{N_{\text{CC}}} \sum_p \sum_{\alpha, \beta} C_p(\alpha; m_{\text{tar}}) C_p^*(\beta; m_{\text{tar}}) \rho_p(\alpha, \beta; t_f)$$

$$\rho(\alpha_M, \beta_N; t) = \langle \alpha_M | \hat{\rho}(t) | \beta_N \rangle$$

**multiexciton  
density operator**

## multiexciton Quantum Master Equation

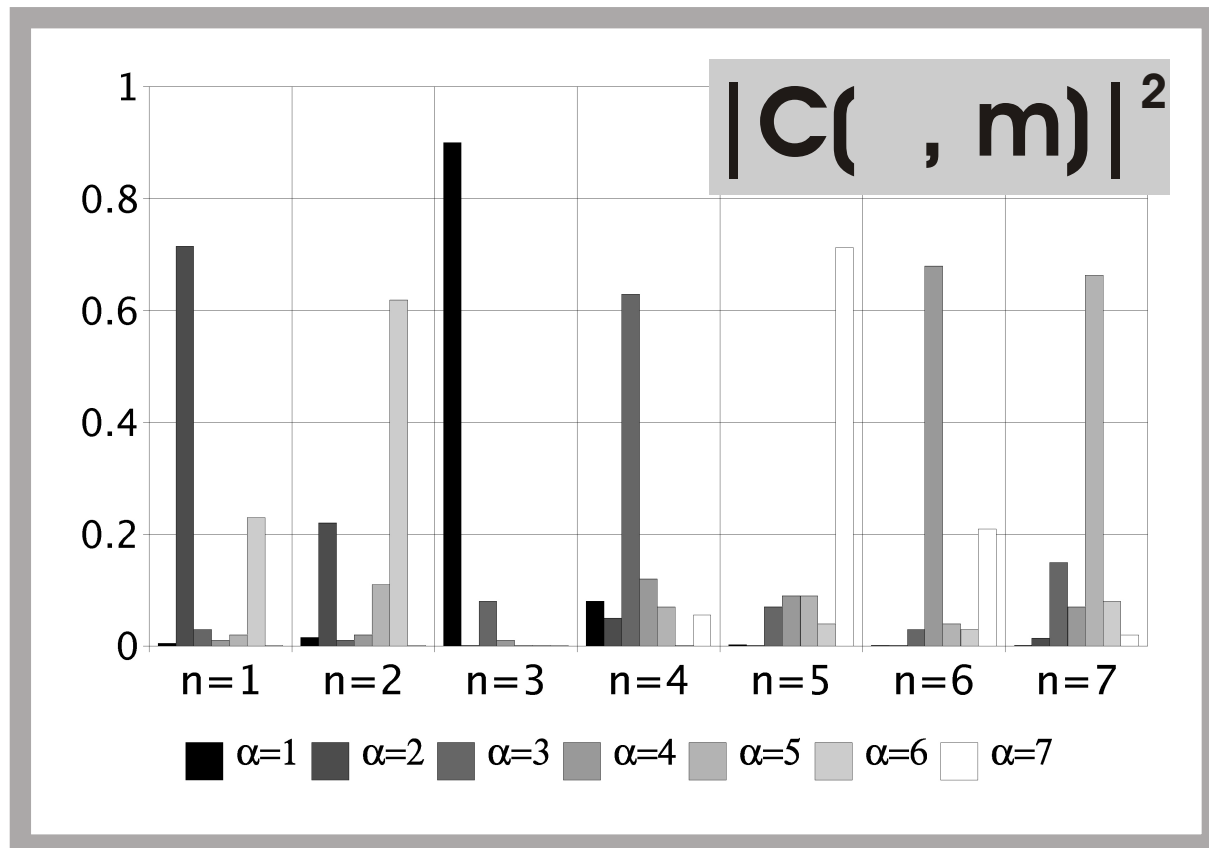
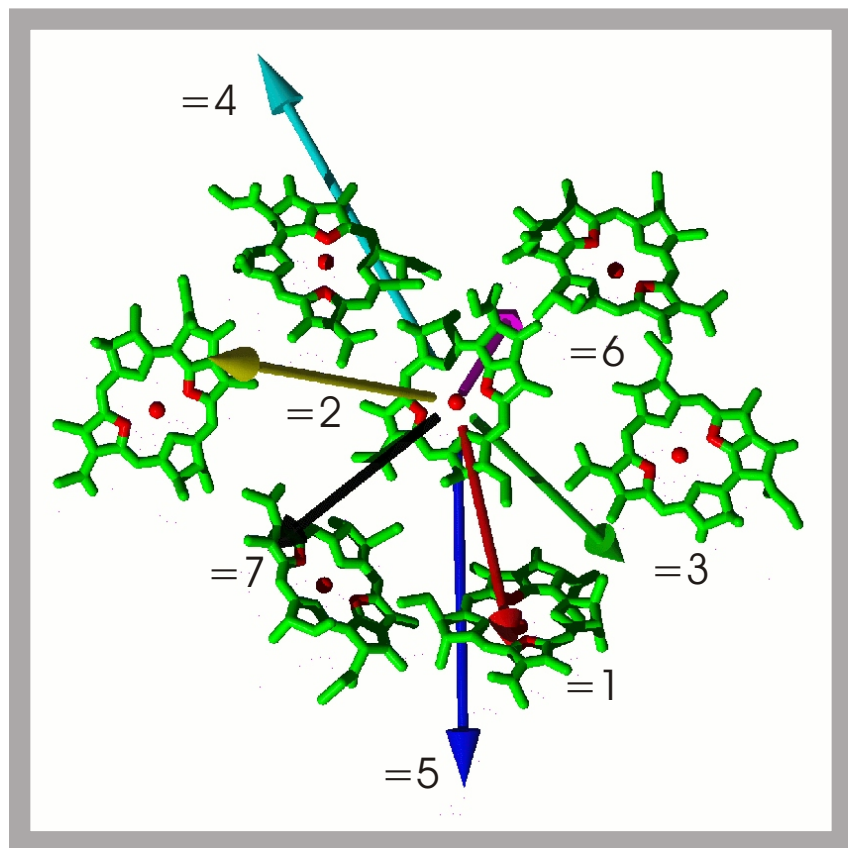
$$\frac{\partial}{\partial t} \hat{\rho}(t) = -\frac{i}{\hbar} [H_{\text{mx}} + H_{\text{field}}(t), \hat{\rho}(t)] - (\mathcal{R}_{\text{mx-vib}} + \mathcal{R}_{\text{eea}}) \hat{\rho}(t)$$

external field  
induced coherent  
motion

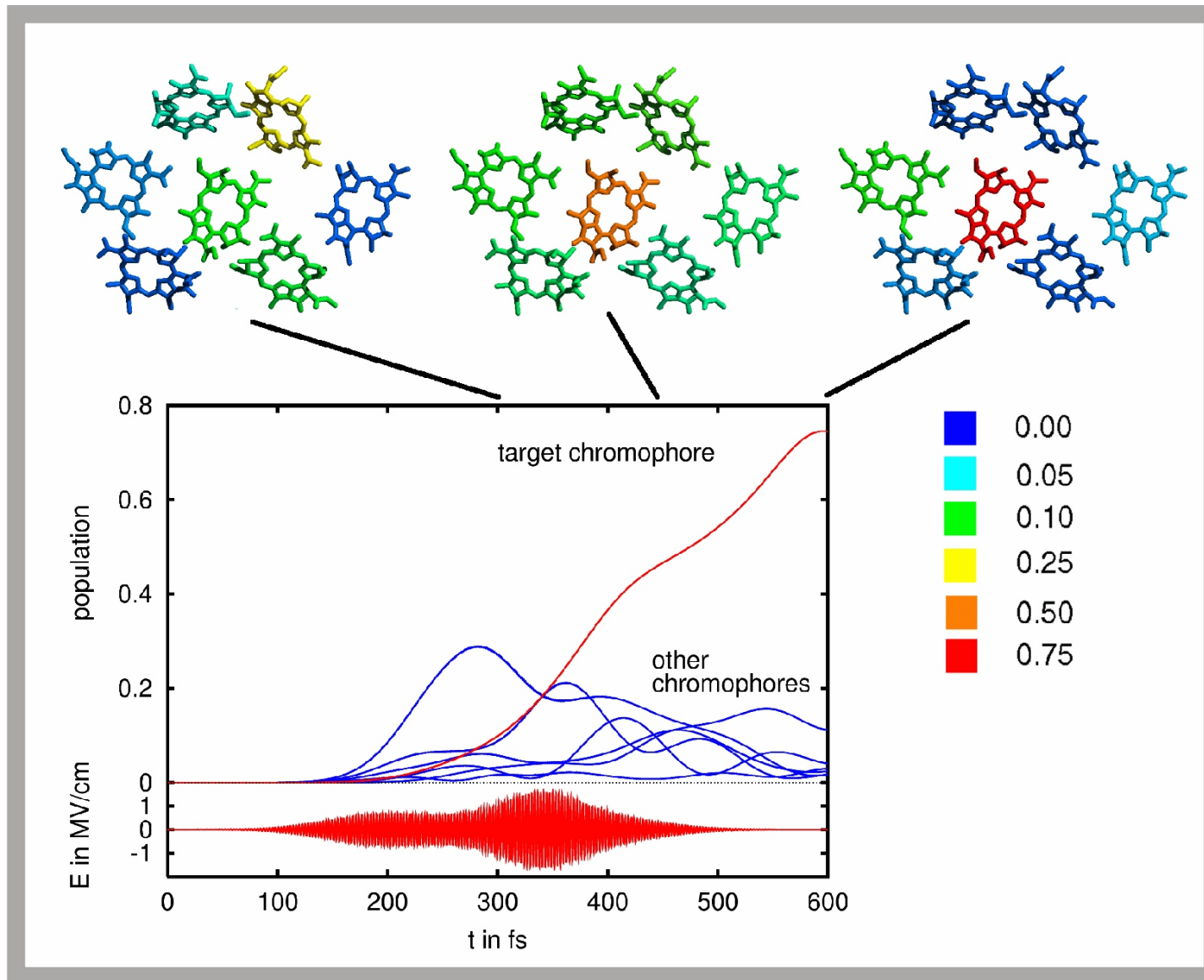
exciton  
relaxation

exciton-  
exciton  
annihilation

# Monomeric Structure of the FMO Complex and Distribution of Exciton Expansion Coefficients



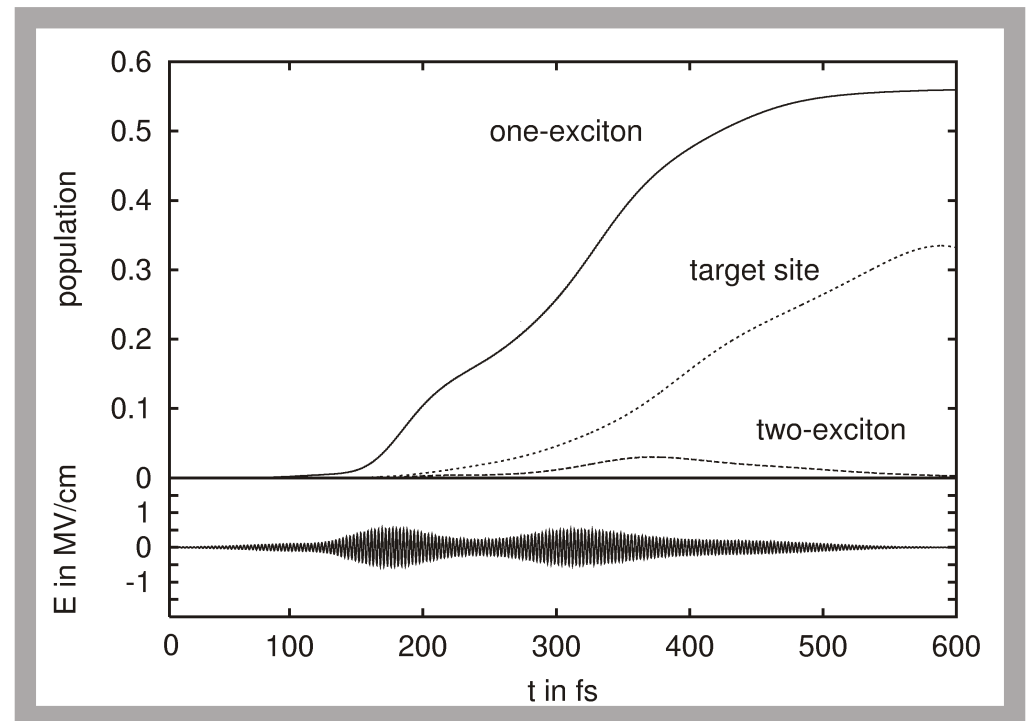
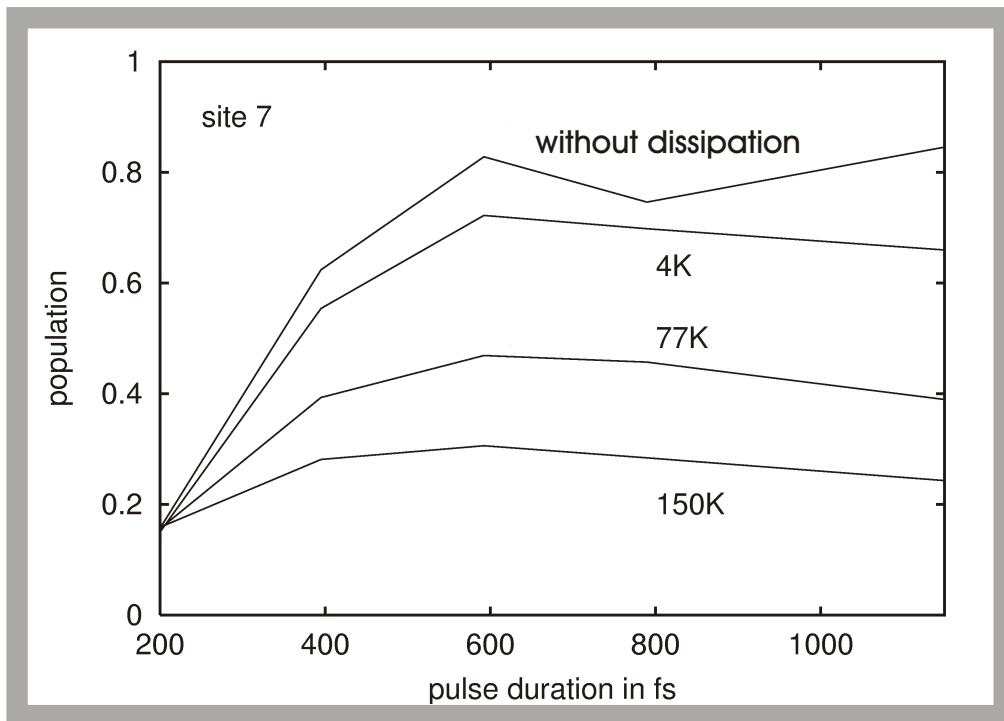
# Laser Pulse Excitation Energy Localization in the FMO-Complex



**B. Brüggemann, and V. M., JPC B 108, 10529 (2004)**



# Excitation Energy Localization at Chromophore $m=7$

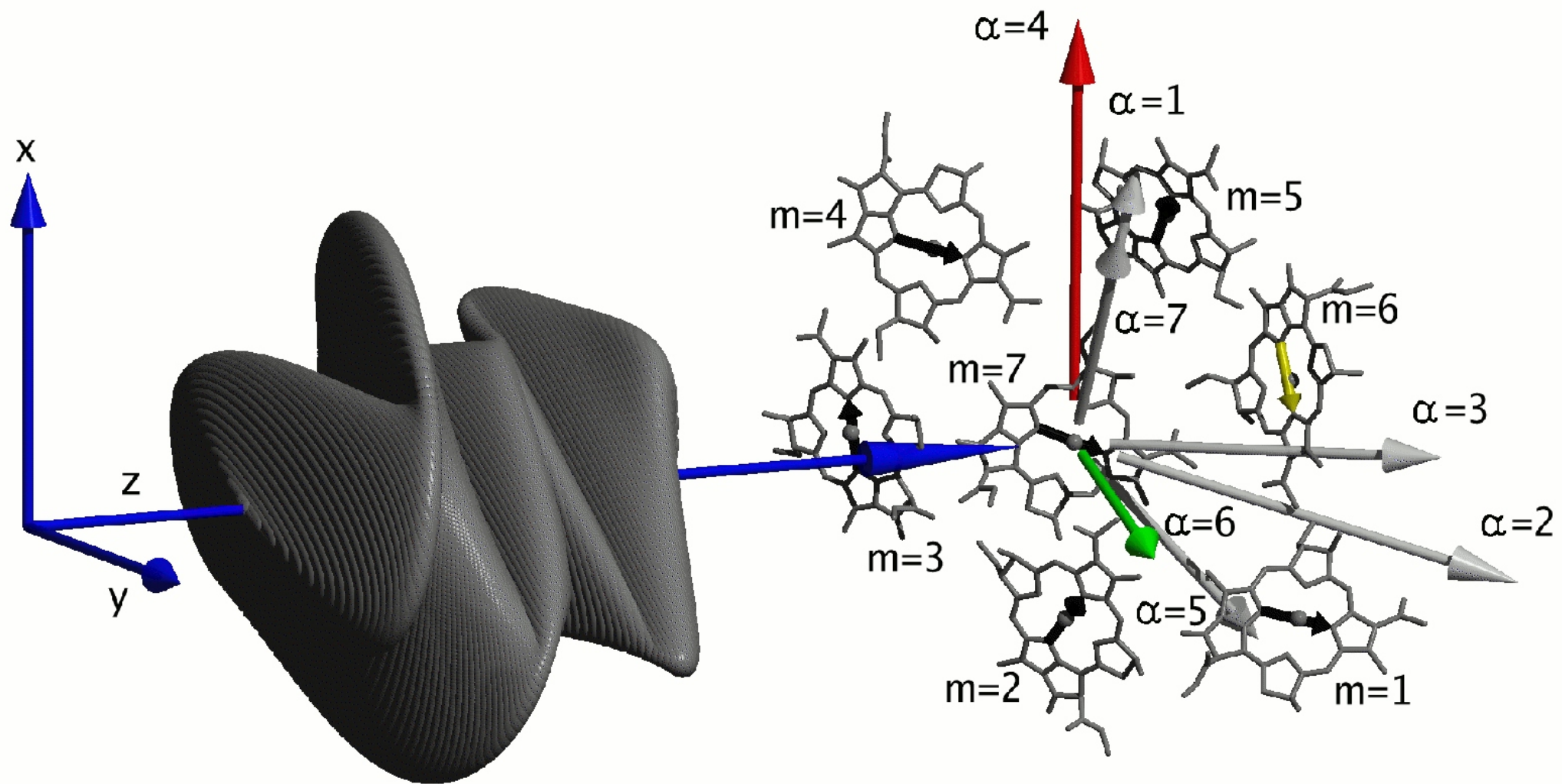


in dependence on

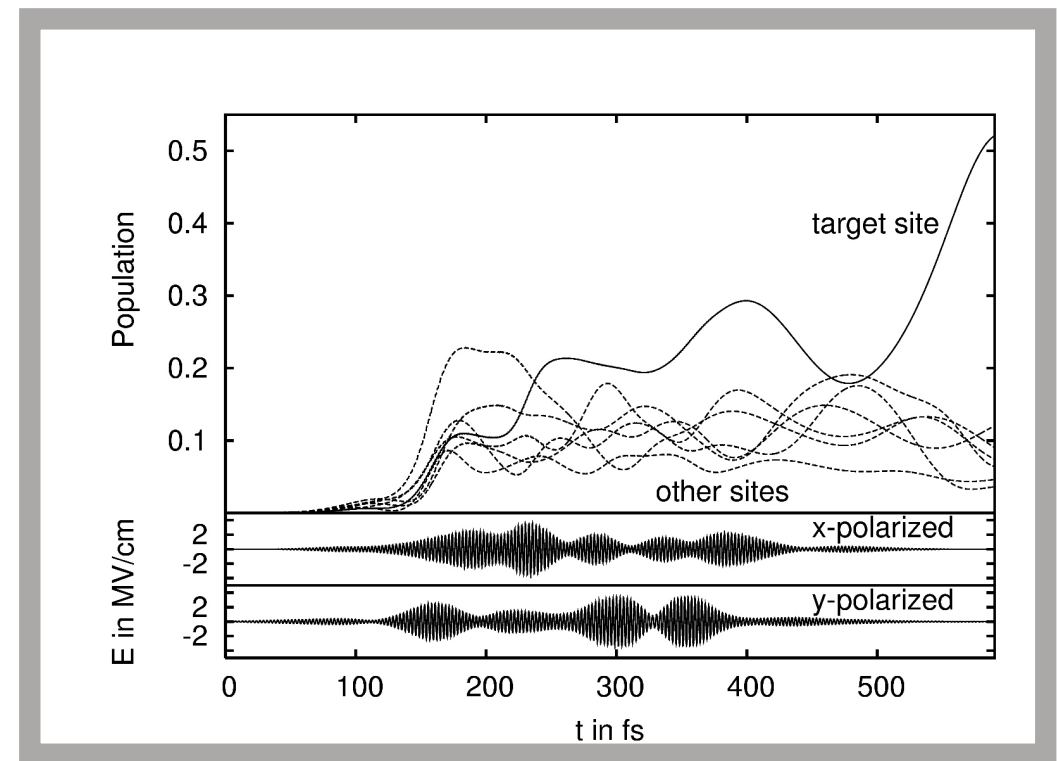
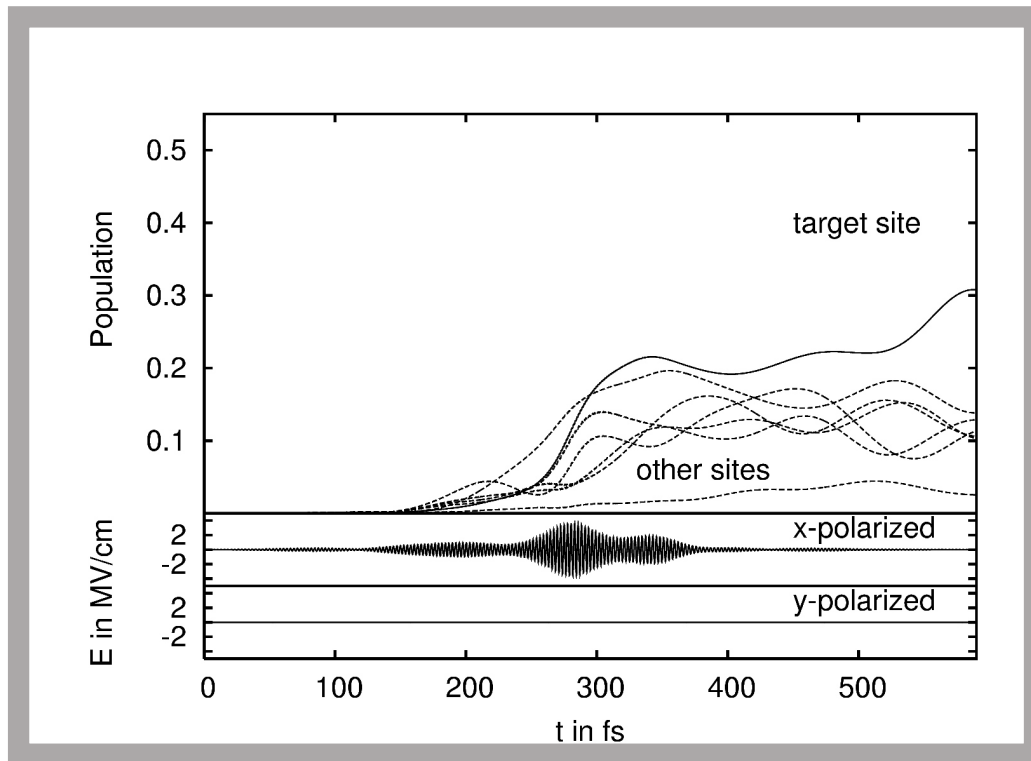
- the control pulse length
- temperature

- including two-exciton states
- at a temperature of 4 K

# Polarization Shaping



# Linear versus circular polarization of the control pulse



- > 10 randomly oriented complexes, -> energetic disorder of  $100 \text{ cm}^{-1}$ ,
- > 4 K, -> neglect of two-exciton levels,

**self-consistency equation for the components of the optimal field**

$$E_{j=x,y}(t) = \frac{1}{N_{CC}} \sum_p \frac{i}{\hbar \lambda} \text{tr}_{\text{mx}} \left\{ \hat{\theta}_p(t; E_x, E_y) [\hat{\mu}_{pj=x,y}, \hat{\rho}_p(t; E_x, E_y)]_- \right\}$$

# **FIFTH EXAMPLE**

# Laser Pulse Control of Multimode Vibrational Dynamics in Pyrazine

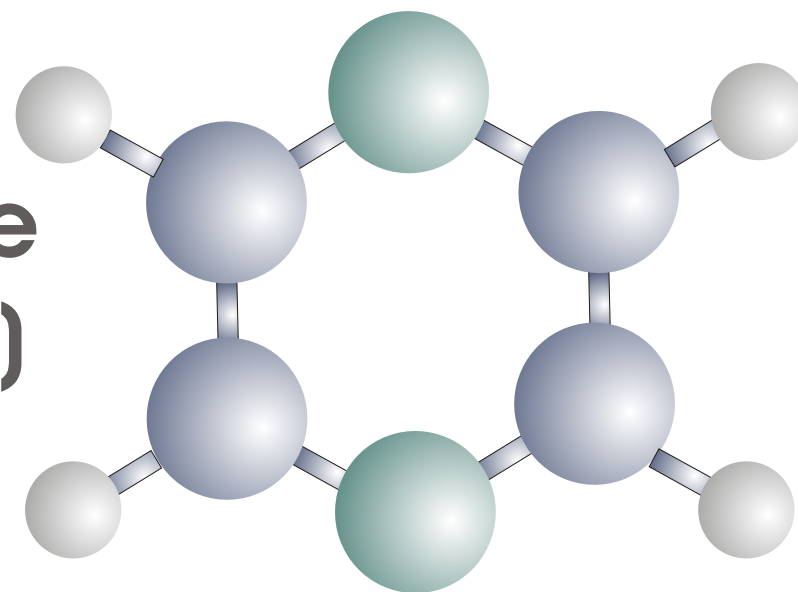
$$\mathcal{O}[\mathbf{E}_c] = \langle \Psi(t; \mathbf{E}_c) | \hat{O} | \Psi(t; \mathbf{E}_c) \rangle$$

plus

Multi Configuration  
Time-Dependent Hartree Method

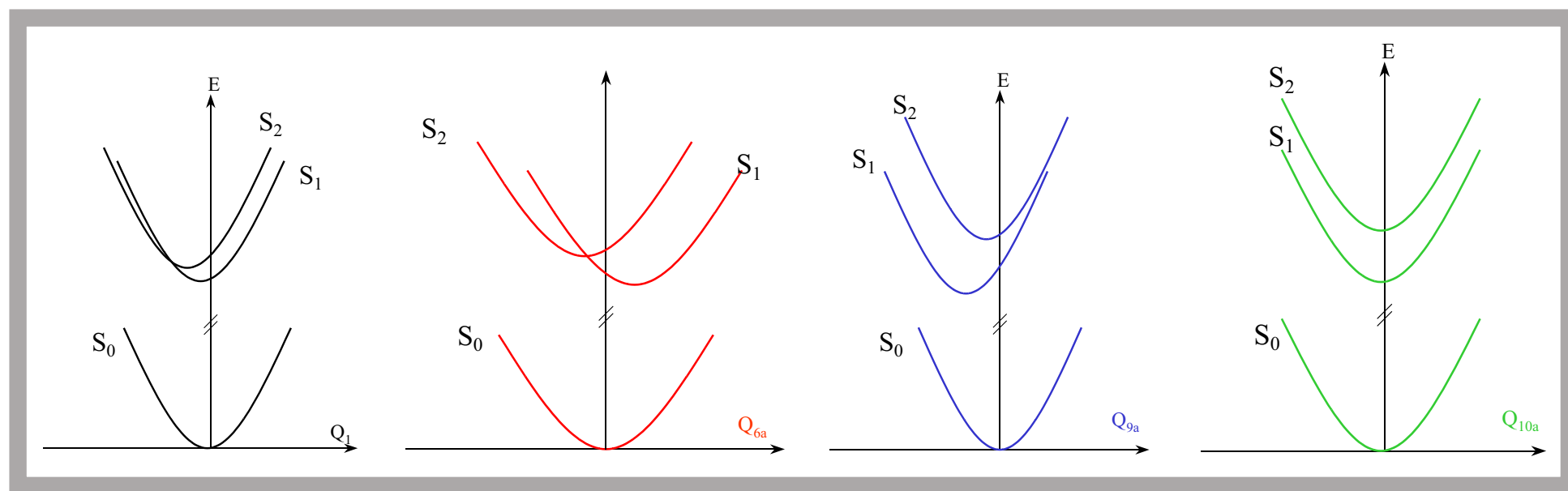
# 4-Mode Model of Pyrazine (vibronic coupling model)

Worth, Meyer, and Cederbaum,  
JCP 109, 3518 (1998)



tuning modes

coupling mode

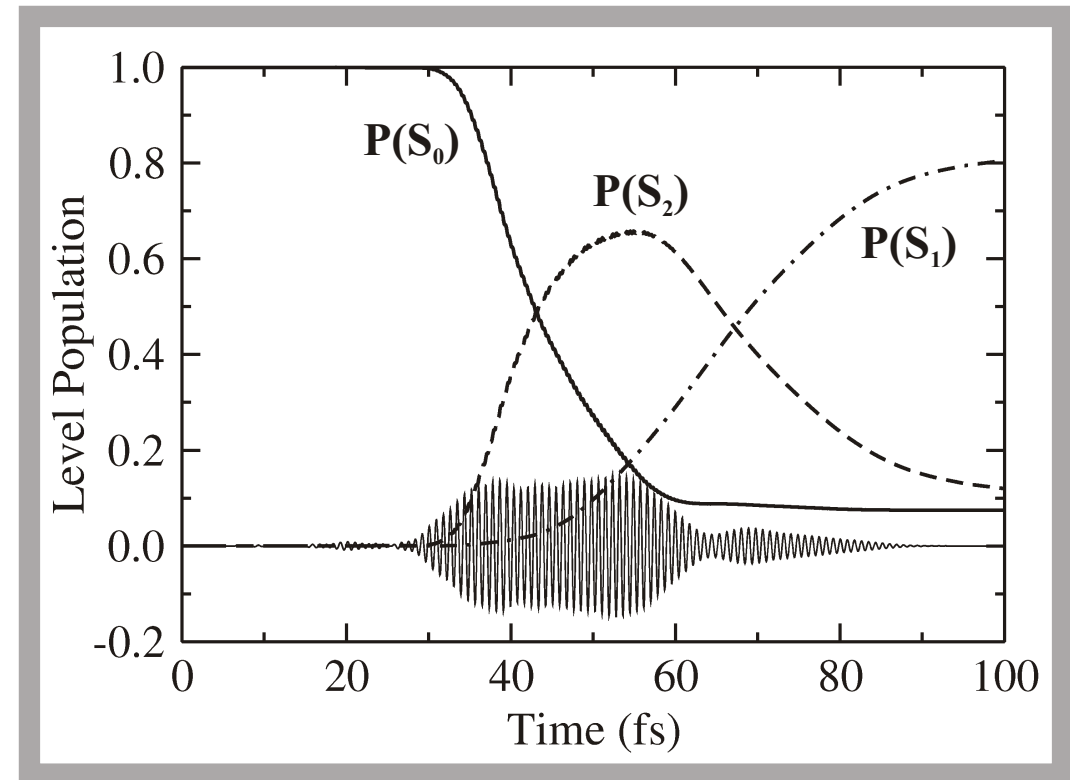
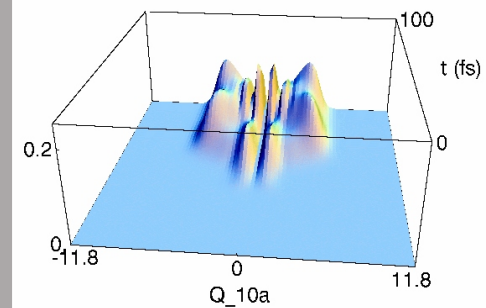
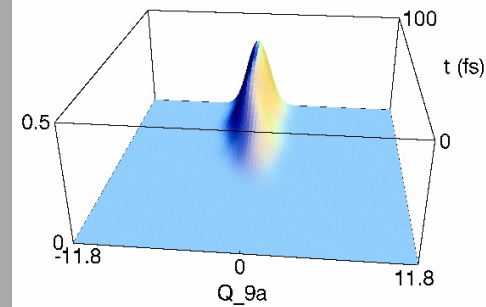
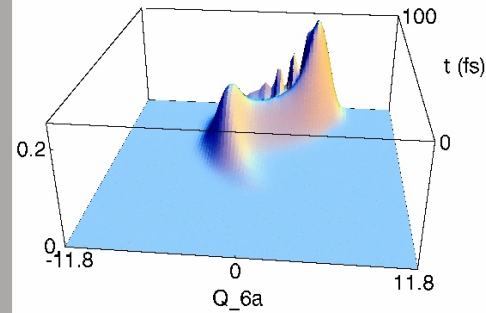
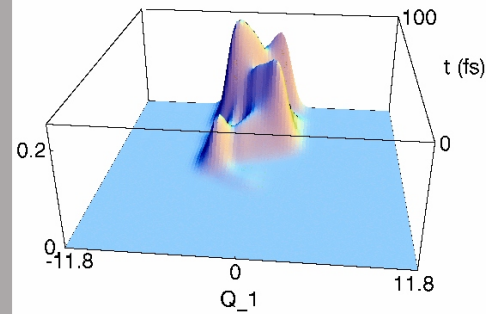


ring stretching

ring bending

out of plane

# Optimization of the overall $S_1$ -population



Reduced probability distribution  
of the four modes

$$P_{S_1}(Q_j, t) = \int dQ' |\chi_{S_1}(Q_1, Q_{6a}, Q_{9a}, Q_{10a}, t)|^2$$

L. Wang, H.-D. Meyer, and V. M., JCP 125, 014102 (2006)

# OUTLOOK



